

Using derivatives with polar functions

Ex. Find the equation of the tangent line to $r = 1 + \sin \theta$

when $\theta = \frac{\pi}{3}$

Still use $y - y_1 = m(x - x_1)$

$$x = r \cos \theta$$

$$x = (1 + \sin \theta) \cos \theta$$

$$x = \left(1 + \sin \frac{\pi}{3}\right) \left(\cos\left(\frac{\pi}{3}\right)\right)$$

$$x = \left(1 + \frac{\sqrt{3}}{2}\right) \left(\frac{1}{2}\right)$$

$$x = \frac{2 + \sqrt{3}}{4}$$

$$y = r \sin \theta$$

$$y = (1 + \sin \theta) \sin \theta$$

$$y = \left(1 + \sin \frac{\pi}{3}\right) \left(\sin\left(\frac{\pi}{3}\right)\right)$$

$$y = \left(1 + \frac{\sqrt{3}}{2}\right) \left(\frac{\sqrt{3}}{2}\right)$$

$$y = \frac{2\sqrt{3} + 3}{4}$$

To find the slope of a tangent line for a polar function

$$y = (1 + \sin \theta)\sin \theta \quad x = (1 + \sin \theta)\cos \theta$$

$$m = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{(1 + \sin \theta)(\cos \theta) + (\cos \theta)(\sin \theta)}{(1 + \sin \theta)(-\sin \theta) + (\cos \theta)(\cos \theta)}$$

$$\text{for } \theta = \frac{\pi}{3} \quad \frac{dy}{d\theta} = \frac{(1 + \sin \frac{\pi}{3})(\cos \frac{\pi}{3}) + (\cos \frac{\pi}{3})(\sin \frac{\pi}{3})}{(1 + \sin \frac{\pi}{3})(-\sin \frac{\pi}{3}) + (\cos \frac{\pi}{3})(\cos \frac{\pi}{3})} = \frac{\left(1 + \frac{\sqrt{3}}{2}\right)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)\left(\frac{\sqrt{3}}{2}\right)}{\left(1 + \frac{\sqrt{3}}{2}\right)\left(-\frac{\sqrt{3}}{2}\right) + \left(\frac{1}{2}\right)\left(\frac{1}{2}\right)}$$

$$= \frac{\frac{2+2\sqrt{3}}{4}}{\frac{-2\sqrt{3}-2}{4}} = \frac{2+2\sqrt{3}}{-2\sqrt{3}-2} = -1$$

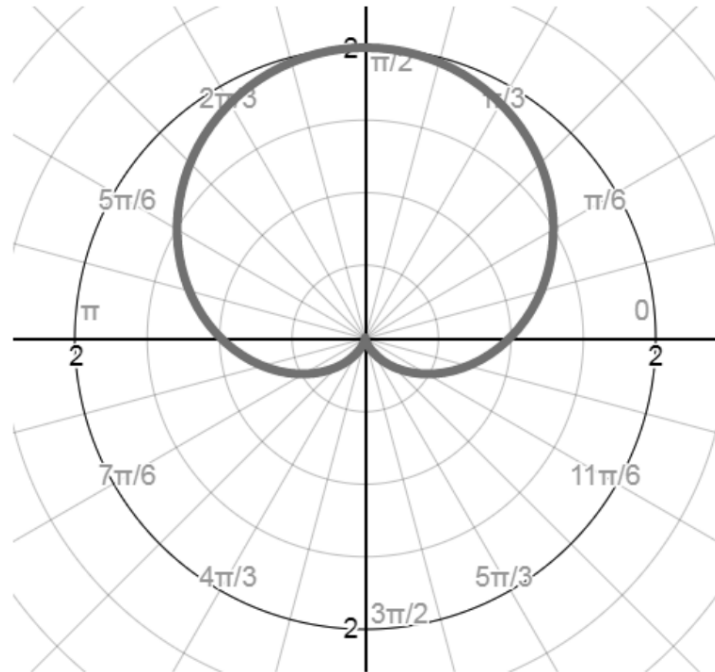
Equation of line tangent to $r = 1 + \sin \theta$ when $\theta = \frac{\pi}{3}$

$$y - \frac{2\sqrt{3}+3}{4} = - \left(x - \frac{2+\sqrt{3}}{4} \right)$$

$$r = 1 + \sin \theta$$

$$y - \frac{2\sqrt{3}+3}{4} = -\left(x - \frac{2+\sqrt{3}}{4}\right)$$

$$y - 1.616 = -(x - 0.933)$$



$$y - \frac{2\sqrt{3}+3}{4} = -\left(x - \frac{2+\sqrt{3}}{4}\right)$$

Consider the polar curve $r = \sin^2(2\theta)$.

What is the equation of the tangent line to the curve r at $\theta = \frac{\pi}{4}$?

Choose 1 answer:

(A) $y - \frac{\sqrt{2}}{2} = -\left(x - \frac{\sqrt{2}}{2}\right)$

(B) $y - 1 = -\left(x - \frac{\pi}{4}\right)$

(C) $y + 1 = -\frac{\sqrt{2}}{2}\left(x - \frac{\pi}{4}\right)$

(D) $y - \frac{\sqrt{2}}{2} = -\frac{\sqrt{2}}{2}\left(x - \frac{\sqrt{2}}{2}\right)$

